

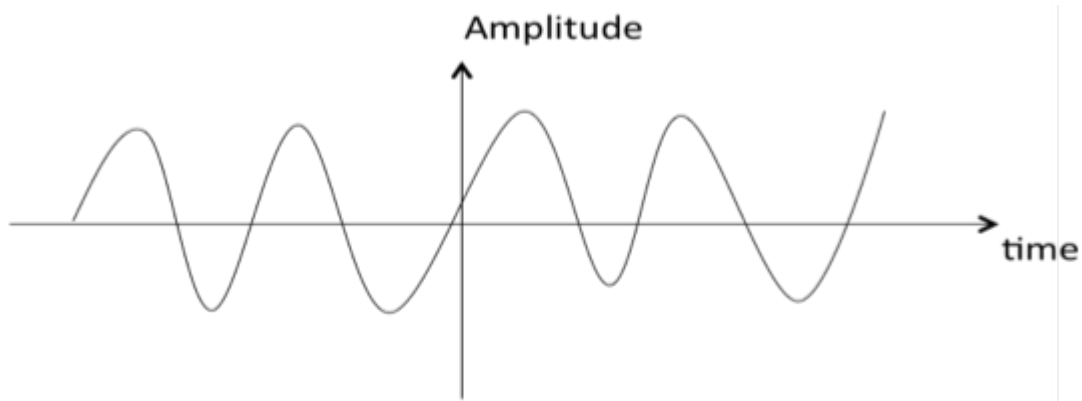
# SIGNALS CLASSIFICATION

Signals are classified into the following categories:

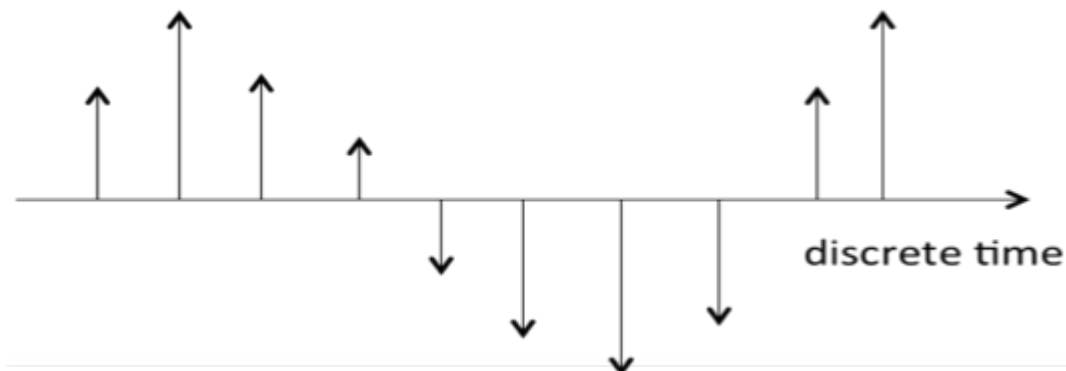
- Continuous Time and Discrete Time Signals
- Deterministic and Non-deterministic Signals
- Even and Odd Signals
- Periodic and Aperiodic Signals
- Energy and Power Signals
- Real and Imaginary Signals

## Continuous Time and Discrete Time Signals

A signal is said to be continuous when it is defined for all instants of time.

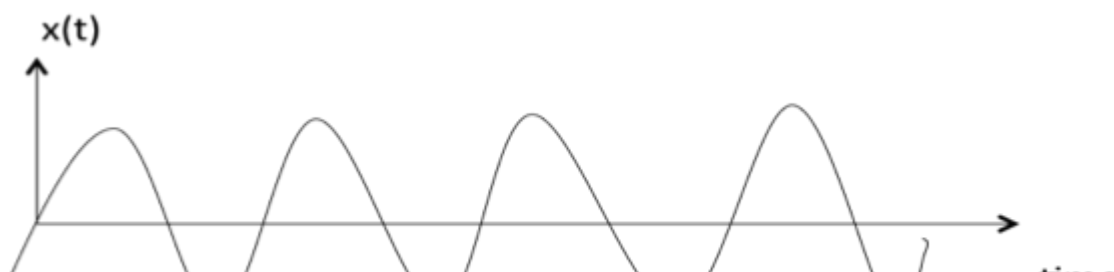


A signal is said to be discrete when it is defined at only discrete instants of time/

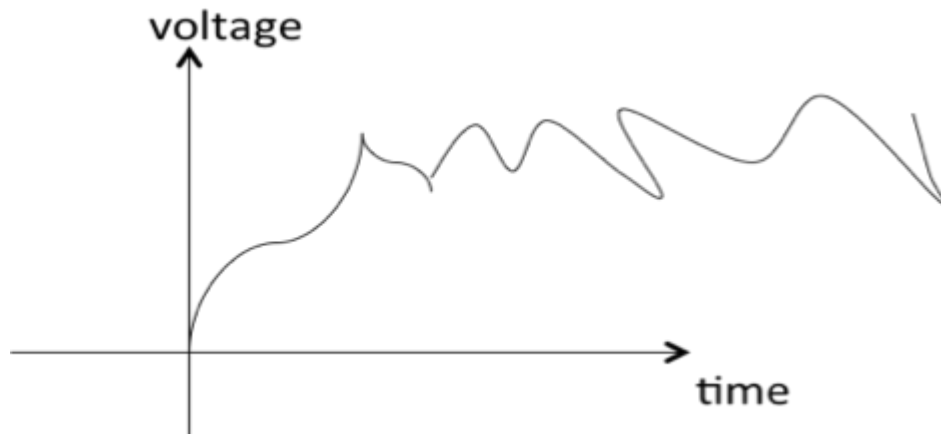


## Deterministic and Non-deterministic Signals

A signal is said to be deterministic if there is no uncertainty with respect to its value at any instant of time. Or, signals which can be defined exactly by a mathematical formula are known as deterministic signals.



A signal is said to be non-deterministic if there is uncertainty with respect to its value at some instant of time. Non-deterministic signals are random in nature hence they are called random signals. Random signals cannot be described by a mathematical equation. They are modelled in probabilistic terms.



### Even and Odd Signals

A signal is said to be even when it satisfies the condition  $x(t) = x(-t)$

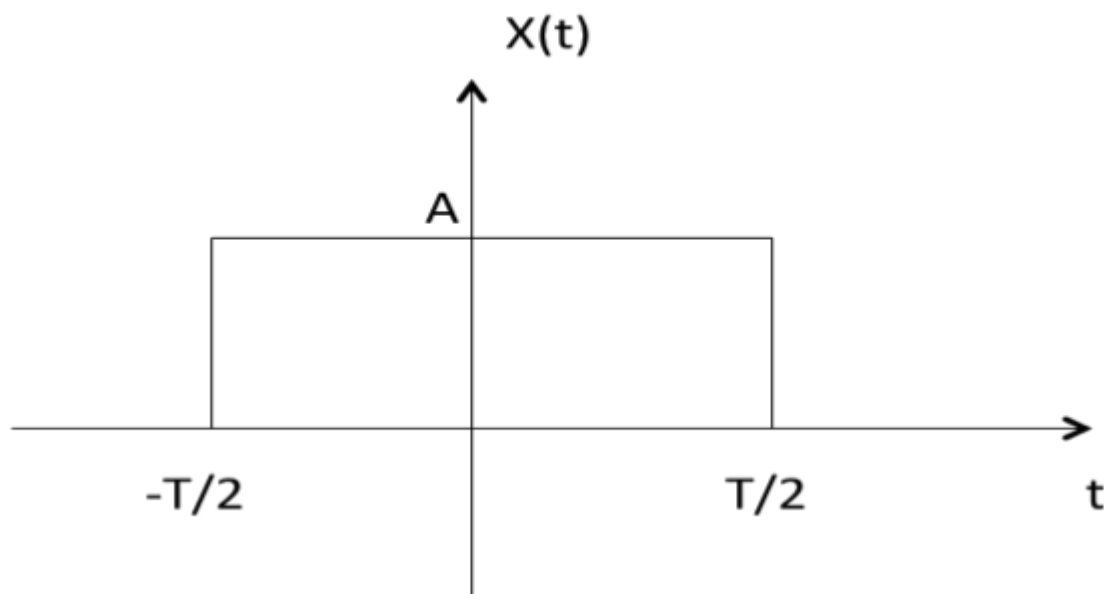
**Example 1:**  $t^2, t^4, \dots$  cost etc.

$$\text{Let } x(t) = t^2$$

$$x(-t) = (-t)^2 = t^2 = x(t)$$

$\therefore, t^2$  is even function

**Example 2:** As shown in the following diagram, rectangle function  $x(t) = x(-t)$  so it is also even function.



A signal is said to be odd when it satisfies the condition  $x(t) = -x(-t)$

**Example:**  $t, t^3, \dots$  And  $\sin t$

$$\text{Let } x(t) = \sin t$$

$$x(-t) = \sin(-t) = -\sin t = -x(t)$$

$\therefore, \sin t$  is odd function.

Any function  $f(t)$  can be expressed as the sum of its even function  $f_e(t)$  and odd function  $f_o(t)$ .

$$f(t) = f_e(t) + f_o(t)$$

where

$$f_e(t) = \frac{1}{2}[f(t) + f(-t)]$$

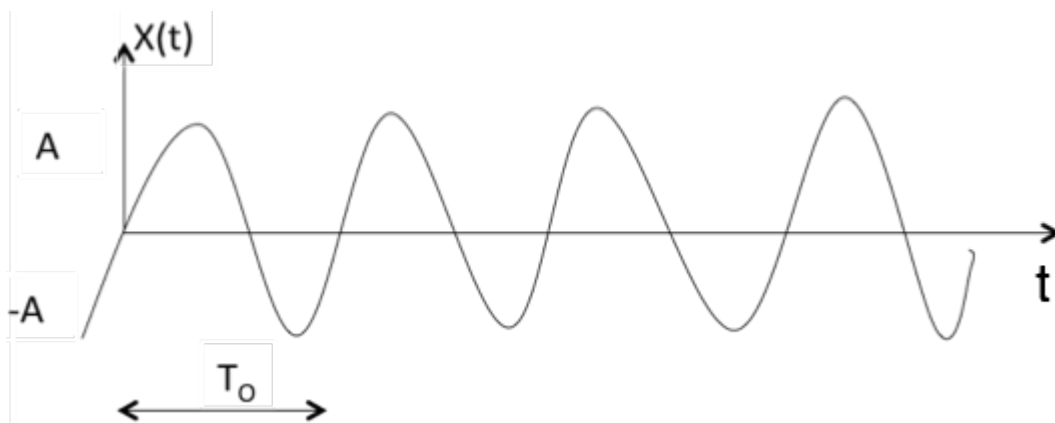
## Periodic and Aperiodic Signals

A signal is said to be periodic if it satisfies the condition  $x(t) = x(t + T)$  or  $x(n) = x(n + N)$ .

Where

$T$  = fundamental time period,

$1/T = f$  = fundamental frequency.



The above signal will repeat for every time interval  $T_0$  hence it is periodic with period  $T_0$ .

## Energy and Power Signals

A signal is said to be energy signal when it has finite energy.

$$\text{Energy } E = \int_{-\infty}^{\infty} x^2(t) dt$$

A signal is said to be power signal when it has finite power.

$$\text{Power } P = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T x^2(t) dt$$

NOTE: A signal cannot be both, energy and power simultaneously. Also, a signal may be neither energy nor power signal.

Power of energy signal = 0

Energy of power signal =  $\infty$

## Real and Imaginary Signals

A signal is said to be real when it satisfies the condition  $x(t) = x^*(t)$

A signal is said to be odd when it satisfies the condition  $x(t) = -x^*(t)$

Example:

If  $x(t) = 3$  then  $x^*(t) = 3^* = 3$  here  $x(t)$  is a real signal.

If  $x(t) = 3j$  then  $x^*(t) = 3j^* = -3j = -x(t)$  hence  $x(t)$  is an odd signal.

**Note:** For a real signal, imaginary part should be zero. Similarly for an imaginary signal, real part should be zero.